Chord Inversions and the Figured Bass Numbers

On an earlier worksheet we looked at a little arrangement of Pachelbel’s Canon in D.

Here, the chords were all in “root position,” meaning that the root of the chord was always on the bottom. Thus, if you wanted a super-quick shortcut to your roman numeral analysis, you could have simply read all of the bass notes and ignored the rest!

However, that is not always how it works. When a note other than the root is in the bass we call it an inversion.

(Note how the upper voices stay the same. It doesn’t matter how the upper voices are stacked - what really matters is the note that’s in the bass.)

We add a little number to our romans to indicate inversion:

I in first inversion = 1\text{ }^6

I in second inversion = 1\text{ }^4
Where do these numbers come from? They are a tradition of musical notation from around 1600 called “figured bass.”

Imagine if you wrote out the triads with just 3 notes in a neat stack, like so:

![root position](image1)

![first inversion](image2)

![second inversion](image3)

Next, you could write numbers to describe the interval shape of the chord:

![5 3](image4)

![6 3](image5)

![6 4](image6)

However, in order to reduce clutter, the Baroque-era music printers eliminated a lot of this information -- so they considered $\frac{5}{3}$ to be “normal” and printed only the information that diverged from it.

![x 6 6](image7)

![x x 4](image8)

Figured bass parts were literally a bass line plus these little numbers. This was enough to tell the harpsichord player what chords to play, and he or she would simply make up the rest of the part much like a jazz pianist accompanies soloists.

So the keyboard part to a Baroque concerto might look like this:

![c d e f g h](image9)

6 6 4
and the harpsichordist would know to play something like this:

\[
\begin{align*}
\text{I} &\quad V^6 & \text{I} &\quad V^6 & \text{I} &\quad I^6
\end{align*}
\]

In order to truly understand how the Baroque musicians were thinking, you have to know that they didn’t have roman numerals, and they didn’t really care much about how the different inversions of a chord were all the same harmony. They cared about the bass note and the different chords that could go with that note.

So, a Baroque keyboardist might look at this and say “that’s a normal C chord, a 5.” He’d look at this:

Finally, he’d see this and say “that’s a C6” or a “six-four chord on C.”

Why do we still use these symbols now? The answer is that Classical music is a deeply traditional discipline. All educated (classical) musicians know these symbols, and so you should too!
Dealing with inversions in analysis

Since it is likely that harmonies in real music will be in the different inversions, it is very important that you take a complete “inventory” of the notes before you decide what roman numeral to give. (I suggest at first that you write out the note-names above the staff and look at them.) Then you look at what part of the triad is in the bass and add an inversion symbol.

You see here that the chord is F-A-C, the V chord in B♭.

The bass has the third of the chord (= 1st inversion.) Thus, you add an inversion symbol, the little “6”.

Always look at the bass for inversions

This may look like a 6/4 chord...

but the bass tells you it’s root position!
Inversion Symbols for Seventh Chords

As with triads, the figured-bass symbols for seventh chords are based on the intervallic structure of the harmony.

<table>
<thead>
<tr>
<th></th>
<th>root position</th>
<th>1st inversion</th>
<th>2nd inversion</th>
<th>3rd inversion</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>3rd on bottom</td>
<td>5th on bottom</td>
<td>7th on bottom</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6</td>
<td>6</td>
<td>6</td>
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<tr>
<td></td>
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<td>5</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3</td>
<td>3</td>
<td>2</td>
</tr>
</tbody>
</table>

Then some redundant numbers are removed. Memorize these symbols:

<table>
<thead>
<tr>
<th></th>
<th>6</th>
<th></th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td></td>
<td>4</td>
<td></td>
</tr>
<tr>
<td></td>
<td>3</td>
<td></td>
<td>2</td>
</tr>
</tbody>
</table>

(I like to think that the numbers tell you where the step is. ⌂ means the step is between 6 and 5, and ⌂ means it is between 4 and 3. It’s not true for ⌂, though.)

(some people also like to just use “2” for third inversion)